



Centre of Excellence on Operations Analyses

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Management of Network Resource Systems with Application to Critical Infrastructure Assessment

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OVERVIEW

A theoretical model and an experimental computer interactive implementation of predicting critical behaviors of large class network-flow systems will be presented.

The model is based on a linear programming approach that allows finding dynamic solutions with multi-criteria optimization of the involved graph-flow problem. Due to ability of **interactive re-computing** with different inputs and control data, an expert, using the proposed solution, can perform an adequate **decision making**.

Possible applications of the present approach in the management of the critical infrastructure in **water supplying system** or **electricity power submission network** are indicated.

GENERAL FLOW DISTRIBUTION MULTI-CRITERIA MULTI-STAGE PROBLEM

Possible results:

Minimization of the total resource insufficiency;

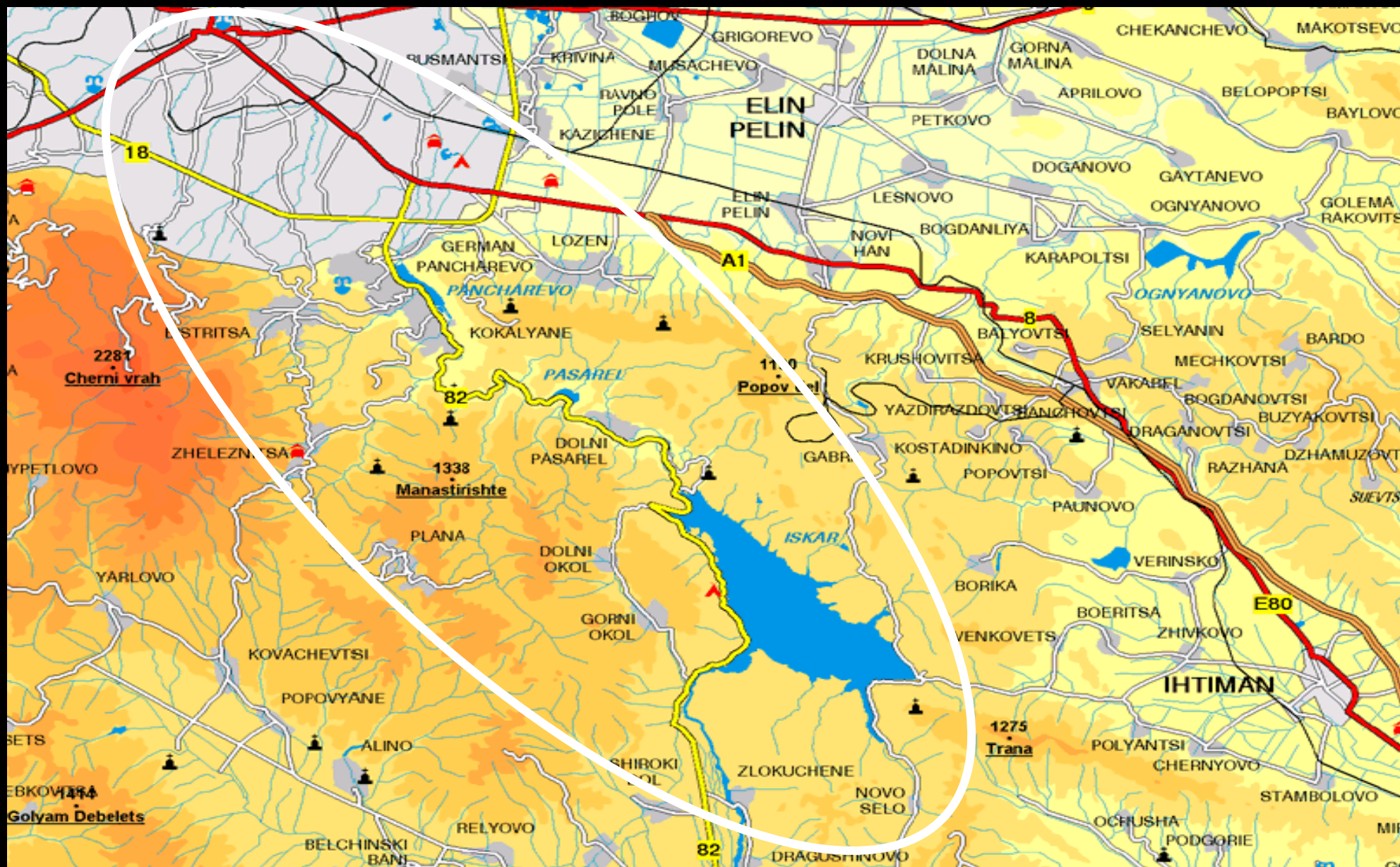
Equalization of resource insufficiency among desired nodes for all time periods;

Maximization of available water;

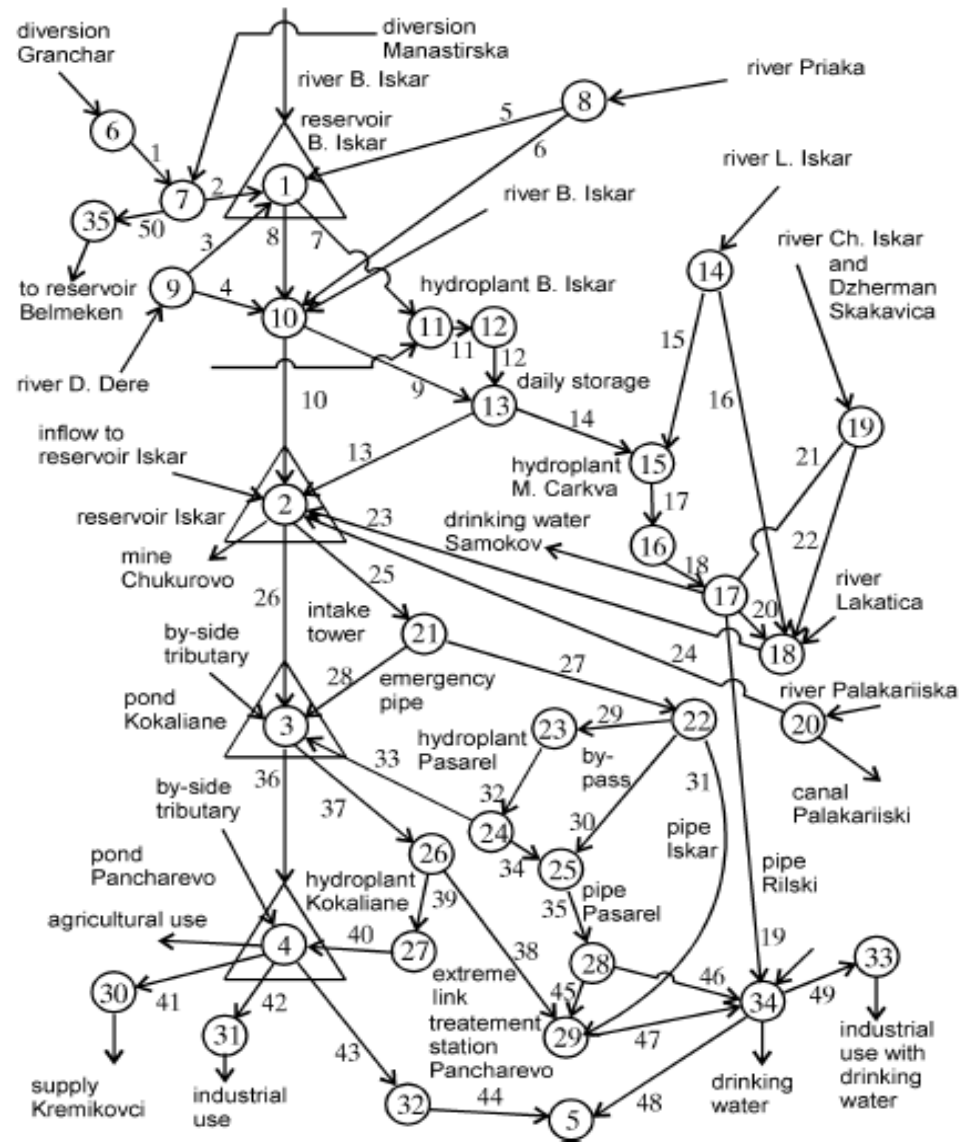
Minimization of total resource losses;

Minimization of the deviation of reservoir storage level from its target storage level.

GEOGRAPHICAL MAP OF THE MODELED REGION



THE GRAPH-FLOWS MODEL



MODEL VARIABLES

The process involves several time steps $t = 1, 2, \dots, T$.

For each node $j = 1, 2, \dots, n$ and for each time moment:
 $t = 1, 2, \dots, T$, the following variables are introduced:

- $u(j,t)$ – amount by which the volume of j -th node increases at the t -th time step;
- $v(j,t)$ – amount by which the volume of j -th node decreases at the t -th time step;
- $r(j,t)$ – current volume.

Some of the nodes are considered as sources:

- $s(j,t)$ – inflow into the j -th node at the t -th time step.

Other nodes are considered as sinks:

- $d(j,t)$ – outflow from the j -th node at the t -th time step.

For each arc $i=1, 2, \dots, m$, and for each time step t :

$f(i,t)$ – flow through the i -th arc at the t -th time step.

MODEL CONSTRAINTS

1. Nodes accumulation: For those nodes j , that are reservoirs, and for any time step t :

$$r(j,t) = r(j, t_0) + \sum\{u(j,k) - v(j,k) : k = t_0, \dots, t\}.$$

2. Continuity equations for each node j and for any time step t :

$$\sum\{f(i,t) : i \in A^+(j)\} - \sum\{f(i,t) : i \in A^-(j)\} + s(j,t) - d(j,t) + u(j,t) - v(j,t) = 0,$$

where:

- $A^+(j)$ is the set of all such i , that the i -th arc is directed into the node j .
- $A^-(j)$ is the set of all such i , that the i -th arc emanates from the node j .

3. Equality and inequality constraints for the variables:

3a. Storage of the reservoirs are within allowable limits:

$$r_{\min}(j) \leq r(j,t) \leq r_{\max}(j).$$

3b. Inflow from sources is equal to available quantities: $s(j,t) = s_{\text{const}}(j,t)$.

3c. Demand values at any demand point: $d_{\min}(j) \leq d(j,t) \leq d_{\text{required}}(j)$.

3d. Pipe capacities (upper bounds) and operational limits (lower bounds):

$$f_{\min}(j) \leq f(j,t) \leq f_{\max}(j).$$

MODEL GOAL FUNCTION

- min: $\sum \{C_1(j,t)d(j,t)\} + \sum \{C_2(j,t)f(j,t)\} + \sum \{C_3(j,t)u(j,t)\} +$
• $\sum \{C_4(j,t)v(j,t)\}$, where:

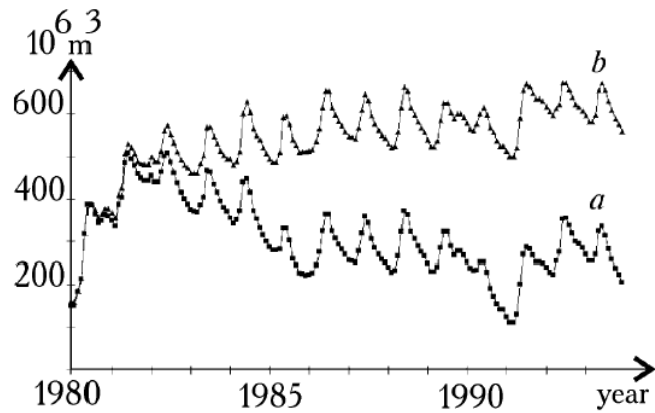
• $C_1(j,t)$, $C_2(j,t)$, $C_3(j,t)$ and $C_4(j,t)$ are constants. Their values are chosen by experts during the interactive mode communication with the modeling system. Typically:

• $C_1(j,t) \ll 0$ or $\gg 0$, depending on node's purpose, where the flows that go out the system. The other constants $C_2(j,t)$, $C_3(j,t)$ and $C_4(j,t)$ are taken close to the init values.

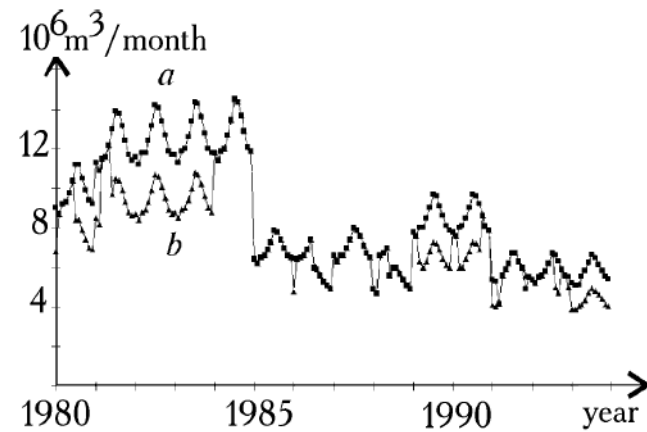
NUMERICAL EXPERIMENTS

Water: Calculations are made for a really existing system including the upper part of Iskar river (near Sofia) for the period of 39 years (1956 - 1994). The model consists of 35 nodes and 50 arcs. The total number of constraints and variables in the resulted LP task were 58036 and 42124 respectively. The computed results showed a good coincidence with the real data. Two main cases (scenarios) are considered: **normal operation - priorities of minimizing shortages** and situation of a **minimizing water losses for a given water volume in the reservoirs** (e.g. dams, ponds, etc.).

RESULTS

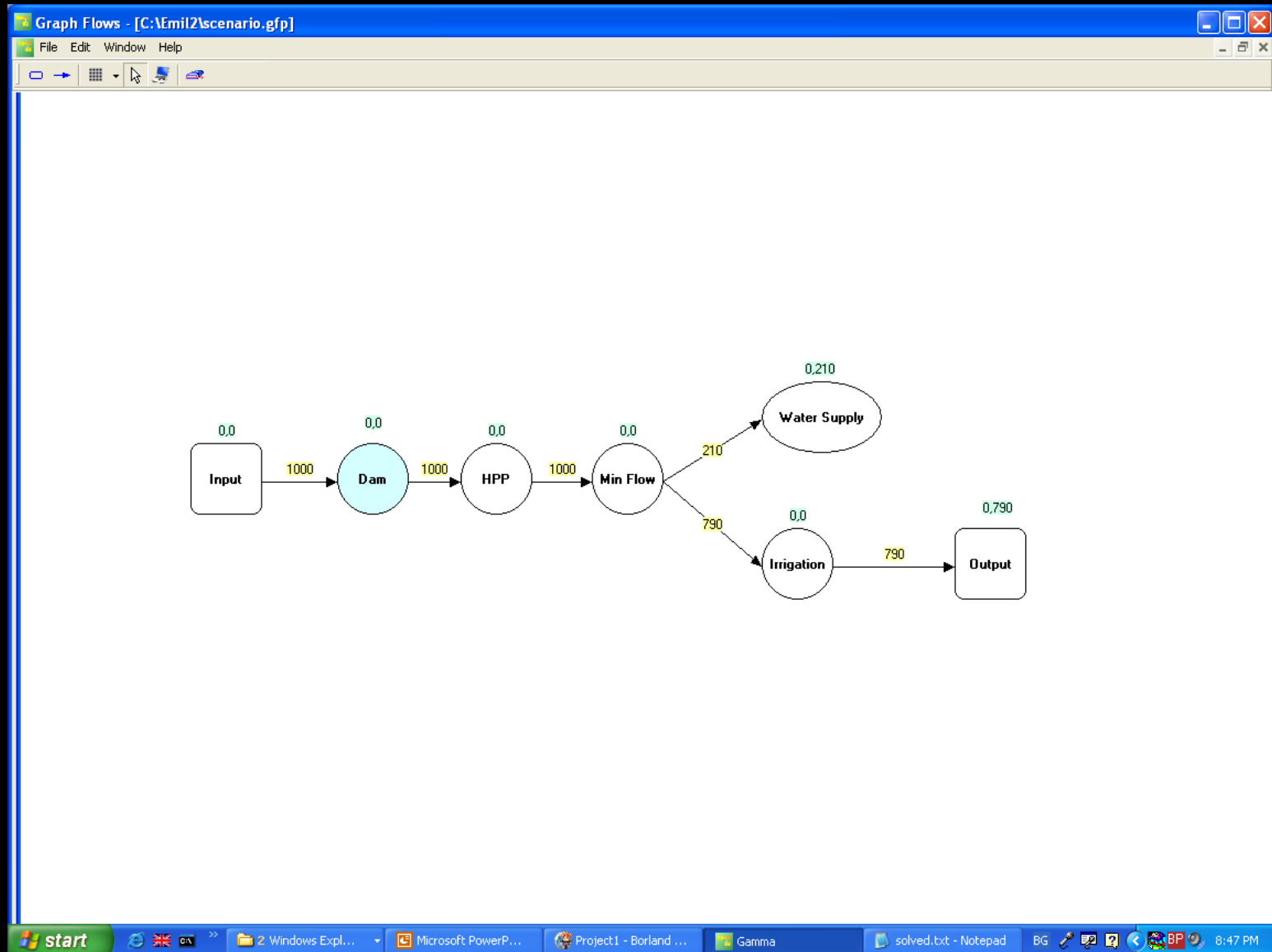


Volume level dynamics of Iskar dam for the period 1980 - 1994



Computed delivery rate of irrigational water at Pancherevo pond - 1980 - 1994

GRAPH-FLOW PROGRAM SCREEN SHOT



THANK YOU FOR THE ATTENTION!